THE DYNAMIC CHARACTERISTICS OF COMPUTER PROGRAMS

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#### THE DYNAMIC CHARACTERISTICS OF COMPUTER PROGRAMS

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One of the goals continuously before us in computer programming is to seek out ways to improve, by shortening, the amount of time taken to solve problems on digital computers. One way to achieve this goal is through more efficient use of the computing facilities which we have today. Monitor systems made a great stride toward this goal by automating the sequencing of jobs through the computing machine, making available on call a number of helpful programs for compiling, assembling, converting, and editing. For a number of years a great white hope has been the multiplexing of programs within a single computing machine. It is hoped that through this technique, idle times of one program may be interleaved with computing times of a second or third program with the combination making more efficient use of the machine than any one of them could have made by itself.

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In multiplex program situations, important questions arise regarding storage allocation, algorithms for choosing the jobs to be run, proper timing of swapping of programs in and out of main memory, and algorithms for switching between programs which are already in memory. In order to answer these questions and to design efficient algorithms, a number of questions about the characteristics of the programs being run need to be answered. Algorithms which operate effectively in one mix of program characteristics will operate inefficiently in other mixes. Some of the central questions involved are:

- 1) The distribution of program sizes.
- 2) The distribution of running times of programs.
- 3) The correlation, if any, between 1 and 2.
- 4) The characteristics of the use of storage by programs.
- 5) Identification of idle intervals within a program, and finding their time distribution.

In category 5, two areas seem apparent. The first is stop time between jobs for tape mounting, finding the next job, dumping the program, etc.; the second, those intervals during which a program waits for I/O actions to complete.

Determining the answers to these questions in current operations will help us know whether program multiplexing is indeed a fruitful area for efficiency gains, and, if it is, help us to find out what kinds of gains we can expect. We should not, of course, neglect the fact that the

job characteristics which we measure today are in some degree dependent on the current method of operation. Programmers, quite correctly, adapt their methods of operation to the system in which they work; any change in the system can be expected to change their habits somewhat. It is entirely possible, of course, that a system design for multiplex program operation will find greater utility and greater solution efficiency than current systems because of the easing of the difficulties of storage allocation and secondary storage utilization.

In order to examine some of these questions in detail, and to find the characteristics of programs using the computer at RAND, a number of statistics have been gathered on actual program runs. Preliminary results of these studies are given below.

## Storage Examination Program

The FORTRAN EXIT program, entered at the end of nearly every FORTRAN job, has been modified to include a routine which examines storage following the execution of each job. Three categories of jobs are not reflected in the statistics gathered by this program:

- 1) Jobs which compile only.
- Jobs so large that they cannot afford storage for this program.

3) Jobs which are dumped from the machine before reaching the EXIT routine.\*

The storage scan routine breaks core into three areas: the program area, below the program break; the common area, above the common break; and unused core, that portion between the program break and the common break. Within such of these areas, five types of cells are recorded:

- 1) Those which are classed as decrement integers. If prefix tag and address of the word are 0, then it is assumed to be a decrement integer.
- 2) Zeros, both plus and minus.
- 3) Instructions which have nine b ts equal to one (AXT, TSX, LXD, SXD, etc.).
- 4) Floating-point numbers--those which have the nine bit equal to one, except for those falling in category 3.
- 5) All other cells which are presumably instructions.

The program punches an accounting card containing these data, and this accounting card is later combined with the ordinary accounting cards produced for the run. Specific additional data gained by combining with the regular accounting cards are log on time, execution time, and number of output lines produced by the program.

Finally, the results of these cards for each job are summarized by a program which produces histograms of the data in various categories.

The limitation of this last category has been eliminated as of 1 February 1964 by including the storage scan routine in the dump routine.

### Preliminary Results

Pata has been gathered with this storage examination program since 30 becember 1963, and histograms have been run on those programs run between 30 December 1963 and 21 January 1964. About 150 jobs were run each day, thouthirds of them in prime shift.

The gross breakdowns of all jobs are shown in Fig. 1. The histograms described below are taken from statistics cards produced by the 60 percent of programs marked in Fig. 1 "FORTRAN Compile and Execute." As can be seen, these jobs represent 48 percent of the running time. The jobs were run on 19 different days during the period.

Figure 2 is the distribution of the number of 0's found in the region of core between the program break and common; thus, it is the best measure we know of the number of cells not used by the program. The bucket, or interval size is given under the heading BKT, with the actual count of jobs and the percentage of jobs falling in each bucket being given in the first two columns. Thus, the figure shows that 64, or 3.7 percent of jobs, did not use between 0 and 1000 cells of core. In this particular bucket, representing very large jobs, the true figure would be larger by perhaps as much as 10 percent since a substantial fraction of jobs are not reflected because they were too large to use this special exit program.

Since the normal complement of FORTRAN library routines occupies approximately 2500 to 3000 cells of memory, it is

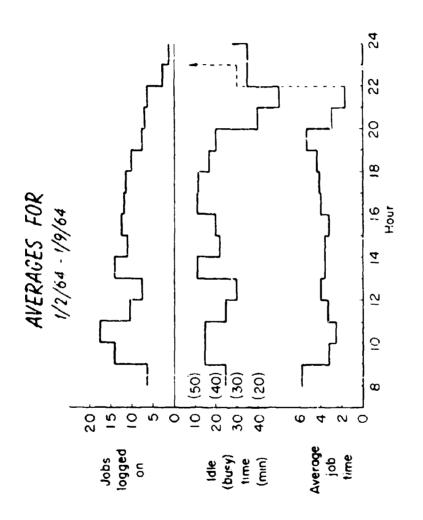


FIGURE 1

HISTOGRAM

```
UNUSED ZERGS INDT USEC, NOT REQUESTED CORE)
COURT PRENT BET
         3.7 OK XXXXXX
   54
         3-1 IK XXXXXX
        2.C 2K NANH
1.4 3K NAN
1.8 4K NANH
1.8 4K NANH
   34
   24
   32
70
         34
   24
   47
   84
         2.0 ICK NEXT
   55
93
         3.2 llk хэрххх
5.4 l2k хэхххххххх
   51
         3.3 L3K XXXXXXX
   35
         2.0 14K XXX
   75
         4.3 ISK XXXXXXXX
         2.2 16K XXXX
1.7 17K XXX
   38
   29
         1.0 18K XX
1.0 19K XX
   18
   18
   28
         1.6 20K HHR
         2.5 21K XXXXX
   36
         2.1 22K XXX
   7.2
         4.2 238 33533333
   e 7
         3.9 24K XXXXXXX
         4.2 25K XXXXXXX
3.7 26K XXXXXXX
   72
   64
52
         3.0 27K XXXXXX
  175
        1C.1 26K XXXXXXXXXXXXXXXXXXXXXXXXX
  169
         KIKKEKKKKKKKKK NPS B.P
```

1.4 30K XXX .0 31K .0 32K

TOTAL

TOTALS

FIGURE 2

not surprising that few jobs leave more than 30,000 cells unused. It is interesting, however, that 36 percent of all programs would have run successfully in an 8K machine.

Two programs, ROCKET and SIMSCRIPT, seem to account for the bulge in storage use in the 12-15K buckets. We should not find it surprising that our machine utilization characteristics are affected by popular programs.

Interestingly, only about 8 percent of programs would not fit in core with some other program commonly available.

Figure 3 presents the number of 0's found anywhere in memory--program area, unused storage, and common. Interesting is the fact that 90 percent of programs leave half of memory or more zero following their execution; 30 percent of programs leave 90 percent of memory empty. Examination of Fig. 3--and Fig. 4 (which shows that the number of floating-point cells found in memory is surprisingly small--70 percent of programs with less than 2000 floating-point numbers) -- makes immediately apparent that many programs contain sparse matrices or allocated but unused tables. Clearly, in the case of sparse matrices, storage allocation techniques of the list variety such as IPL-V possesses would be of great value; and, in the second case, a dynamic storage allocation scheme providing storage only when requested would save large amounts of storage for use by other programs.

Figure 5 shows actual program sizes as determined by the number of instructions in the program and unused region.

## TOTAL OF ZERO CELLS

COUNT	PRCNT	BKT	PISTOGRAM
0	0		
	• 0	OK	
0	.0	I K	
0	.0	2 K	
0	• C	3 K	
0	-0	4 K	
ļ	. 1	5 K	
l	. 1	6 K	
3	• 2	7 K	
2	- 1	BK	u.
8	. 5	9 K	
9	. 5	ick	<b>A</b>
4	• ?	11K	
14	. 8	15K	
57	3.3		XXXXXX
28	1.6	14K	
26	1.5	15K	
44			XXXX
36	2.1		XXXX
51	5.3	-	XXXXXXXX
59	3.4		XXXXXX
43	2.5		XXXX
70	4.0		XXXXXX
78	• •		XXXXXXX
70	4.C	23K	
108			KKKKKKKKK
55	• •		XXXXXXXX
54	5.4		XXXXXXXX
144			XXXXXXXXXXXXX
144			XXXXXXXXXXXXXXXX
382	22.1	-	***************************************
121	7.0		XXXXXXXXXX
C		31K	
0	•0	32K	
1732	T	DTAL	

FIGURE 3

FIGURE 4

```
TOTAL CF PRESUMEC INSTRUCTIONS, PRCG . UNLSED
COUNT PRENT BKT
                                          HISTOGRA4
  £ 7
     3.9 16 2222222
    552
 256
 169
 113
     160
 65
  55
  55
     2.7 LOK XXXXX
  47
  54
     3.1 llk xxxxxx
     .9 12K XX
  16
     .1 14K
     .5 15K X
     4.0 16X XXXXXXXX
     1.2 17K AA
.1 18K
 2 C
     .2 19K
  0
     .0 20K
     .C 21K
     .0 22K
  Ō
  e
     .0 24K
  0
     .0 25K
     .0 26K
```

.0 27K

.0 29K .0 30K

.0 32K

TOTAL

0 0

0 Ō

1732

FIGURE 5

With the exception of the popular SIMSCRIPT and ROCKET, which appear in the 16,000 instruction bucket, most programs are very small--50 percent being less than 4000 instructions long. This fact, coupled with the total allocation in Fig. 2, forces one to conclude that large amounts of storage are assigned to tables.

Figure 6 presents the data of Fig. 5 (weighted by straight multiplication) by the execution time of the program involved. Since very little change in the distribution is noted, we conclude that it is not possible to tell from the number of instructions in a program how long it will execute. I'm sure no one will be surprised by this fact.

Figure 7, however, plots the number of unused 0's weighted by execution time. This is the same data as in Fig. 6 and shows a very pronounced shift toward the larger programs near the top of the chart. The peak of Fig. 6 in the small program region is completely missing from Fig. 7. Thus, we note the strong correlation (as shown again in a different way below) between the size of the programs and their execution time. It seems to be a strong characteristic of programs that if the space requested is small, they will run a short time. If it is large, they will run a long time.

In the 5K and 8K buckets may be seen the pronounced effect of popular programs. This time, not particularly big ones but long running.

## TOTAL INSTRUCTIONS, WEIGHTED BY AXECUTE TIPE

```
COUNT PRENT BKT
                                            HISTOGRAM
     182
6933
1902
2552
         KKKKKKKKKKKKKKK NA
     10.6
     1С.9 7к жижжижжижжийнийний
2606
      1.1 SK XX
 259
 796
      3.3 9K XXXXXX
 941
      3.9 10K XXXXXXX
      6.4 lik xxxxxxxxxxxxxxxx
2005
 330
      1.4 12K XXX
  3
25
      .0 13K
      -1 14K
 146
      .6 15K X
 312
      1.3 16K XXX
 let
      .7 17K X
      .1 16K
  19
      .2 19K
  42
      -0 2CK
  C
      .0 21K
      .0 22K
   Ö
   0
       .0 23K
      .0 24K
      .0 25K
   0
      .0 26K
      .0 27K
      .0 28K
   Q
      .0 29K
      .0 30K
      .0 31%
   0
      .0 32K
   0
240C3
       TOTAL
```

FIGURE 6

#### UNUSED ZEROS, WEIGHTED BY EXECUTE TIME

```
COUNT PRENT BKT
                                                               HISTOGRAM
 2038
        8.5 ОК ХХХХХХХХХХХХХХХХХХХХХХ
 1720
        7-2 IK XXXXXXXXXXXXXXX
  978
        4.1
              ZK XXXXXXX
  343
        1.4
             3K XXX
  390
             4K XXX
        1.6
 6345
       10.0 SK XXXXXXXXXXXXXXXXXXXXXXX
  483
        2.C 6K XXXX
 1027
        4.3
             7K XXXXXXXXX
       15.1 BK XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX
 3630
  315
        1.3 9K XXX
         .8 ICK XX
  188
 1193
        5.C 11K XXXXXXXXX
  813
        3.4 12K XXXXXX
  621
        2.6 13K XXXXX
  463
        1.9 14K XXXX
  689
        2.9 15K XXXXXX
  516
        2.1 16K XXXX
        1.6 17K XXX
.4 18K X
  374
  108
         .4 19K X
  105
  2C7
         .9 20K XX
  483
        2.0 21K XXXX
  555
        2.3 22K XXXXX
  784
        3.3 23K XXXXXXX
 1256
        5.2 24K XXXXXXXXX
        1.5 25K XXX
  372
  145
         .6 26K X
        2.7 27K XXXXX
3.2 28K XXXXXX
1.6 29K XXX
  644
  762
  375
         .1 30K
   26
         .0 31K
    ٥
          .0 32K
24CC3
          TOTAL
```

FIGURE 7

Figure 8 again demonstrates this shift by plotting the total number of 0's weighted by execution time. It, too, reinforces the thought that big programs run a long time and little programs run a short time. And remember, these are not instructions in the program but total allocation of storage. Thus, while we cannot tell how long a program might run by asking how many instructions the program contained, we can tell by asking how many instructions plus how many cells of tables does it contain.

Figure 9 plots the number of jobs arriving at the 7090 in each hour of the day. Here the bucket column represents an hour. Noteworthy are the first and second shift lunch-hour dips at 12:00 and 20:00 hours. Also apparent is the slow rise from early morning to full production at 10:00, and from lunch time until full production again at 2:00. It seems a full stomach is a bad thing for programmers. Perhaps we should hire only hungry programmers.

Production of output for printing is a crucial one in most installations, being one of the primary bottlenecks hindering fast turnaround time. Figure 10 plots the number of jobs occurring in each category of output volume. From the figure, it can be seen that more than 50 percent of jobs can be printed using a single 600-line-a-minute printer in a time equivalent to the running time of the job. Perhaps this is an indication that we should return to on-line printing. We are certainly okay if we have sufficient

## TOTAL ZERGS, WEIGHTED BY EXECUTE TIME

COUNT	PRCNT	BKT	FISTOGRAP	4
o	.0	OK		
0	-0	1 K		
0	.0	2 K		
0	-0	3 K		
0	.0	4 K		
23	- 1	5K		
26	- 1	6 K		
33	- 1	7 K		
29	. 1	8 K		
160	. 7	9 K	X	
85	_	10K		
127		11K		
141		12K		
733			XXXXXX	
133	•6	-		
1807			XXXXXXXXXXXXX	
2115			KXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	
1278			KKKKKKKK	
3496	14.6	18K	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	
1038	_	_	XXXXKKXK	
770		-	XXXXX	
1723			X X X X X X X X X X X X X X X X X X X	
813			XXXXXX	
1135			XXXXXXXX	
1854			XXXXXXXXXXXX	
1118	4.7	25K	XXXXXXXX	
770			אאגאנא	
1866	7.8	27K	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	
786	3.3	28K	XXXXXX	
1766	7.4	29K	XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX	
198		30K	XX	
0	•0	31K		
0	-0	32K		
24003	T	OTAL		

FIGURE 8

E

ŧ

ONTINES - EACH RUCKET IS AN HOUR

```
COUNT PRONT BET
                                                         HISTOGRAM
   17
        1.0
             KK NO
   16
         . 9
             KK XI
    7
             2K X
    9
         • 5
             3K X
    2
         • 1
             4K
         • 0
             5 K
         . 1
             6K
    0
         .0
             7 K
   13
         . 8
             8K XX
        4.6
   60
            KKKKKKKK NP
        9.6 LOK XXXXXXXXXXXXXXXXXXXXX
  166
        KKKKKKKKKKKKKKK Nii 8.8
  152
  107
        4xxxxxxxxxx 351 5.6
        7.3 13K XXXXXXXXXXXXXXXXX
  126
       173
  170
       KKKKKKKKKKKKKKKK 371 8.P
       XXXXXXXXXXXXXXX No. 0.P
  166
       KKKKKKKKKKKKKKK NTI 0.8
 139
       KKKKKKKKKKKK NAI 6.6
 113
 104
       KKKKKKKKKKK NPI 0.6
  42
       2.4 20K XXXXX
  65
       3.8 ZIK XXXXXXXX
  36
       2.1 22K XXXX
  28
       1.6 23K XXX
   0
        .0 24K
   0
   0
        .0 26K
   0
        .0 27K
   0
        .0 28K
   0
        .0 29K
   0
        .0 30K
   Ü
        .0 31K
        *0 35K
1732
        TOTAL
```

FIGURE 9

ALL JEAS

```
7C 18L S
              ERECUTION LINES IN THOUSANDS OF LINES
COUNT FRENT BET
                        F1510G#AP
```

1732

FOTAL

FIGURE 10

storage available with which to buffer the output so that bursts of printed output from the program can be smoothed for presentation to the printer.

Most installations have limits on the number of lines which may be produced during the critical prime shift hours; thus, those jobs which appear on this curve near the tail end--the high output jobs--can be expected to occur during the non-critical third shift.

Figure 11 weights 7090 on-time by the number of execution lines produced. Thus, it is a map of the printer load during the day. Compare this figure with Fig. 9 and note the attempt of the noon-time operator to run the jobs which produce more output, possibly the longer jobs, during his rather hectic session at the machine.

#### Running Times

Figure 12 presents a number of different distributions of running times of jobs taken from various studies. Although there is a large variation in the number of jobs run in any particular time category, it is clear that the great bulk of jobs run for only a short amount or time. The limitations usually imposed at computing installations make this no surprise. Still, it is a bit surprising to find 60 percent or more programs executed in less than two minutes.

Figure 13's scatter diagram presents a correlation of the execution-time data together with the total program-size

#### POTALS

# CHILDE HEIGHTED BY EXEC LINES IN ICCO'S OF LINES

MISTOGRAM

FIGURL 11

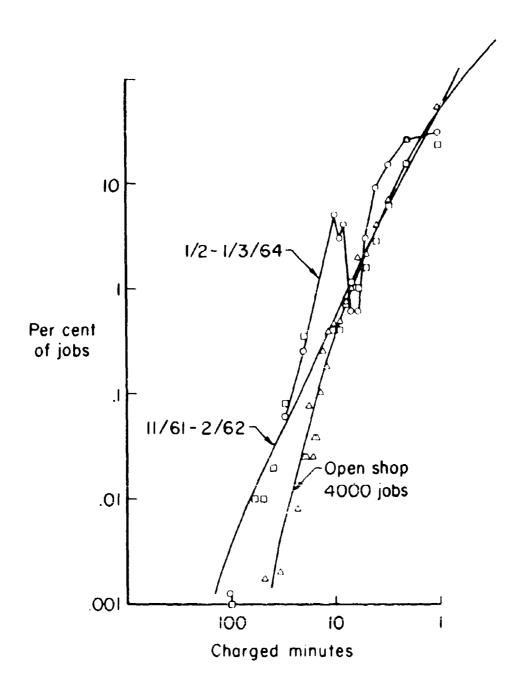


FIGURE 12

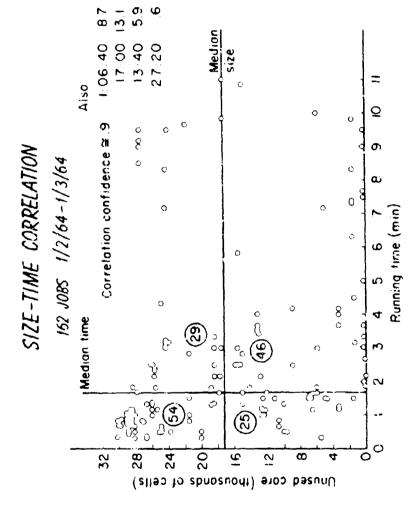


FIGURE 13

data. As was seen in the histograms, there is a substantial correlation between job size and running time. Note particularly the large group of jobs in the under-one-minute running time and less than 4000-in-words of storage category. Again, since many of the jobs on the opposite end of the spectrum--the large end--are run late at night, we find small, short jobs a pronounced characteristic of prime shift jobs.

#### Unused Time

In our supposedly advanced monitor controlled job shops, we find substantial portions of unused time during even the busiest hours of the day. Figure 14 is an example of this characteristic. The center curve plots the average for 6 days of unused time during each hour. Note that we are never able to utilize more than 50 minutes out of each hour. Tape mounting, finding jobs, and other delays attributable to semi-manual operation are reflected here. It is probably unreasonable to expect that any non-automatic system would be able to do better.

Figure 14 also plots the number of jobs logged on each hour and the average time occupied by each job during that hour. Interestingly, between 10:00 in the morning and 8:00 in the evening the average job time does not vary substantially from the overall average time, although late at night large jobs were indeed run.

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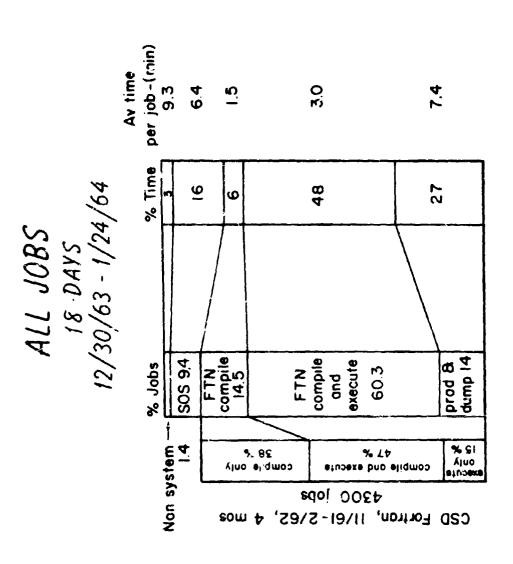


FIGURE 14

It should be pointed out that the wait times reflected here are the non-charge times—and thus do not reflect waiting time within the program for tape I/O transmission, rewinds, backspaces, and waits for the operator to dump the job, dial in tapes, or complete other manual operations.

Figure 15's scatter-diagram plots for each hour one point on coordinates of number of jobs logged in, and idle time for the hour. This diagram shows no correlation between idle time and number of jobs, indicating that the job-shop monitor is working fine but that certain manual delays are unavoidable and are independent of the number of jobs being processed.

#### Summary

I believe that the above statistics demonstrate that substantial gains are achievable through a multiplexed program mode of operation. Substantial numbers of programs exist in the small-time and small-program size categories to insure that programs can be easily found which will fit available time-space slots. Further, because of these factors, rather simple allocation algorithms will be sufficient. We need not look far ahead in the input stream to find a suitable job to fit the dimension available in either time or space.

We have also shown that there are substantial gains to be achieved in storage allocation areas--both in list processing styles of storage allocation in which both the

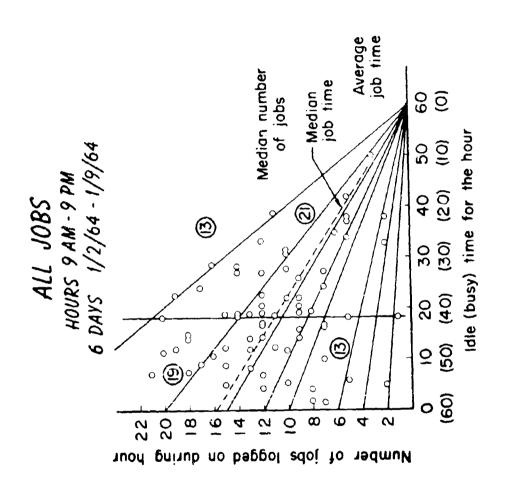


FIGURE 15

location and its contents are important data in the storage reference, and in the dynamic storage requests in which tables of nominal size are expended to fill the needs of the program as it executes.

It would not be overstating the case to predict that an efficiency or through-put gain of 100 percent is achievable through implementation of these techniques.